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**Fear the Turtle**

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# Some Topics in Simulation Optimization

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National Science Foundation Workshop

College Park, MD

May 24-25, 2010

# Research Streams

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- Simulation Optimization
  - Discrete: model-based methods, computing budget allocation
  - Continuous: stochastic gradient estimation
- Global Optimization
  - Model Reference Adaptive Search (MRAS) [see Jiaqiao Hu]
  - connecting to stochastic approximation/gradient search [see Jiaqiao Hu]
  - particle filtering framework [see Enlu Zhou]
- Markov decision processes (MDPs)
  - Simulation-based framework, adaptive sampling
  - Population-based & model-based algorithms

Note: joint work with Steve Marcus, Hyeong Soo Chang, Jian-Qiang Hu, Chun-Hung Chen, L. Jeff Hong, Yongqiang Wang, et al.

# What makes simulation optimization hard?

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- Key: OBJECTIVE FUNCTION contains quantities that must be estimated from stochastic simulation output
- Ordinary optimization can concentrate on the search.
- Due to the stochastic nature of the problem, there is both search and evaluation.
  
- Trade-off between  
**finding more candidate solutions**  
vs. **obtaining a better estimate of current solutions**  
i.e., **finding  $\arg \min_{\theta \in \Theta} J(\theta)$**  vs. **estimating  $J(\theta)$**

# Stochastic Gradient Estimation Approaches

approach	# simulations	key features	disadvantages
IPA	1	highly efficient, easy to implement	limited applicability
other PA	often > 1	model-specific	more difficult to apply
LR/SF	1	requires only model input distributions	possibly high variance
WD	2*(# appearances of parameter)	requires only model input distributions	possibly large # simulations
SD FD (one-sided)	2*p p+1 (dimension)	widely applicable, model-free	noiser, biased, large # simulations
SP	2	widely applicable, model-free	noiser, biased

Acronyms: infinitesimal perturbation analysis, likelihood ratio/score function, weak derivatives, symmetric/finite differences, simultaneous perturbations

# Selected Relevant References

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