## IEMS 326, Homework 1, Due 4/6/2011

Please see the homework policies in the syllabus, especially about charts and spreadsheets.

- 1. (Simple Calculations) Use a 6% discount rate for this problem.
  - a) What is the present value of \$3.14 invested 15 years ago?
  - b) Newnan et al. chapter 5 problem 4.
  - c) Newnan et al. chapter 5 problem 8.
- d) Calculate the present value if you receive 30 payments of \$100 starting 5 years from today
- e) Calculate the present value if you pay \$10/yr for 3 years with the first payment being today, and then starting a year from today you will receive \$6/yr for 6 years.
- 2. Modify the social security spreadsheet to answer the following questions. *Do not show your work and do not turn in the spreadsheet.*
- a) Produce a chart showing how the 2050 trust fund balance (y-axis) changes with the real rate of return (x-axis). At what real rate of return is the 2050 balance zero?
- b) Suppose that the current recession temporarily reduces the labor force participation among 18-64 to 65% but that it recovers in 2011 (to its baseline value of 76.7%). How does this change the year at which the trust fund becomes negative? What if the labor force participation remains depressed at 65% until 2012 and only recovers in 2013?
- c) Suppose the population 18-65 grows an additional 500,000 a year due to immigration, that is add 500,000 to the population in 2010, 1m to the population in 2011, 1.5m to the population in 2012, etc. How would that affect the 2050 balance of the trust fund?
- d) Suppose the tax rate is reduced by 100 basis points<sup>1</sup> in 2010-2011 (to stimulate the economy). What is the effect on the 2050 balance of the trust fund?
- e) Come up with one additional scenario to explore. Describe the scenario and results (in complete sentences).
- 3. (Saving for college tuition) Suppose that on 9/1/2015, you and your significant other have a child. You plan to open a 529 account at that point to save for the child's future college expenses. The total cost of attending Northwestern for the 2010-2011 academic year is \$56,006. Assume that this cost will increase by 4% annually. You plan to put money into the 529 account each year starting from the child's birth to their 18<sup>th</sup> birthday, at which point they start college. Each year you will increase your contribution by 2% (as you get raises at your job). Assume that the investment return of the account is 3% annually; that expenses fall at the beginning of the academic year (September 1<sup>st</sup>), and that your child will graduate in 4 years. How much should be in the 529 account when your child starts college (just after you make the contribution on their 18<sup>th</sup> birthday)? How large should your first contribution be (on the child's day of birth)? How much extra do you need to save if your child will take 5 years to graduate? *Build a spreadsheet and highlight your answers*.

 $<sup>^1</sup>$  A basis point is  $1/100^{th}$  of a percent, or 0.0001. For example, adding 100 basis points to a tax rate of 12.4% means increasing the tax rate to 13.4%. This terminology helps us to be more precise: if I said, increase the tax rate by 1%, you might wonder whether I meant 12.4% + 1% = 13.4% or  $12.4\%*(1.01) \approx 12.5\%$ .